

Die Erhaltungssätze für Masse, Drehmoment und Energie können jeweils in differentieller Form oder Integralform geschrieben werden:

Differentielle Form

$$\frac{\partial \rho}{\partial t} + \operatorname{div} \cdot (\rho \vec{v}) = 0$$

$$\rho \frac{\partial \vec{v}}{\partial t} + (\rho \vec{v} \cdot \nabla) \vec{v} = \vec{f}_0 + \operatorname{div} \mathbf{T} = \vec{f}_0 - \operatorname{grad} p + \operatorname{div} \mathbf{T}' \quad (3.33)$$

$$\rho T \frac{ds}{dt} = \rho \frac{de}{dt} - \frac{p}{\rho} \frac{d\rho}{dt} = -\operatorname{div} \vec{q} + \mathbf{T}' : \mathbf{D}$$

Integralform

$$\frac{\partial}{\partial t} \iiint \rho \, d^3V + \iint \rho (\vec{v} \cdot \vec{v} \, e \, cn) \, d^2A = 0 \quad (3.34)$$

$$\frac{\partial}{\partial t} \iiint \rho \vec{v} \, d^3V + \iint \rho \vec{v} (\vec{v} \cdot \vec{n}) \, d^2A = \iiint f_0 \, d^3V + \iint \vec{n} \cdot T \, d^2A \quad (3.35)$$

$$\begin{aligned} \frac{\partial}{\partial t} \iiint \left(\frac{1}{2} v^2 + e \right) \rho \, d^3V + \iint \left(\frac{1}{2} v^2 + e \right) \rho (\vec{v} \cdot \vec{n}) \, d^2A = \\ - \iint (\vec{q} \cdot \vec{v} \, e \, cn) \, d^2A + \iiint (\vec{v} \cdot \vec{f}_0) \, d^3V + \iint (\vec{v} \cdot \vec{n} \, T) \, d^2A. \end{aligned} \quad (3.36)$$

Der ∇ -Operator in kartesischen Koordinaten:

$$\vec{\nabla} = \frac{\partial}{\partial x} \vec{e}_x + \frac{\partial}{\partial y} \vec{e}_y + \frac{\partial}{\partial z} \vec{e}_z, \quad \operatorname{grad} f = \vec{\nabla} f = \frac{\partial f}{\partial x} \vec{e}_x + \frac{\partial f}{\partial y} \vec{e}_y + \frac{\partial f}{\partial z} \vec{e}_z$$

$$\operatorname{div} \vec{a} = \vec{\nabla} \cdot \vec{a} = \frac{\partial a_x}{\partial x} + \frac{\partial a_y}{\partial y} + \frac{\partial a_z}{\partial z}, \quad \nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2}$$

$$\operatorname{rot} \vec{a} = \vec{\nabla} \times \vec{a} = \left(\frac{\partial a_z}{\partial y} - \frac{\partial a_y}{\partial z} \right) \vec{e}_x + \left(\frac{\partial a_x}{\partial z} - \frac{\partial a_z}{\partial x} \right) \vec{e}_y + \left(\frac{\partial a_y}{\partial x} - \frac{\partial a_x}{\partial y} \right) \vec{e}_z$$